

Laplace transform tables.

$f(t)$	$\mathcal{L}\{f(t)\}$
$\sin kt$	$\frac{k}{s^2 + k^2}$
$\cos kt$	$\frac{s}{s^2 + k^2}$
e^{at}	$\frac{1}{s - a}$
$\sinh kt$	$\frac{k}{s^2 - k^2}$
$\cosh kt$	$\frac{s}{s^2 - k^2}$
$e^{at} f(t)$	$F(s - a)$
$\int_0^t f(\tau)g(t - \tau)d\tau$	$F(s)G(s)$
t^α	$\frac{\Gamma(\alpha + 1)}{s^{\alpha+1}}, \alpha > -1$
t^n	$\frac{n!}{s^{\alpha+1}}, n \text{ a positive integer}$
$t^n f(t)$	$(-1)^n \frac{d^n}{ds^n} F(s)$
$f^{(n)}(t)$	$s^n F(s) - s^{(n-1)} f(0) - \dots - f^{(n-1)}(0)$

Useful formulas.

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\sin(A \pm B) = \sin A \cos B \pm \sin B \cos A$$

$$\cos A \cos B = [\cos(A + B) + \cos(A - B)]/2$$

$$\sin A \sin B = [\cos(A - B) - \cos(A + B)]/2$$

$$\cos^2 x + \sin^2 x = 1$$

$$\cos x = \frac{e^{ix} + e^{-ix}}{2} \quad \sin x = \frac{e^{ix} - e^{-ix}}{2i}$$

$$\cosh x = \frac{e^x + e^{-x}}{2} \quad \sinh x = \frac{e^x - e^{-x}}{2}$$

$$\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt, \text{ recurrence relation: } \Gamma(x+1) = x\Gamma(x). \text{ Convergence requirement: } x-1 > -1 \text{ or } x > 0.$$